

# Low $x$ , low $Q^2$ $A_1^p$ and $g_1^p$ status report

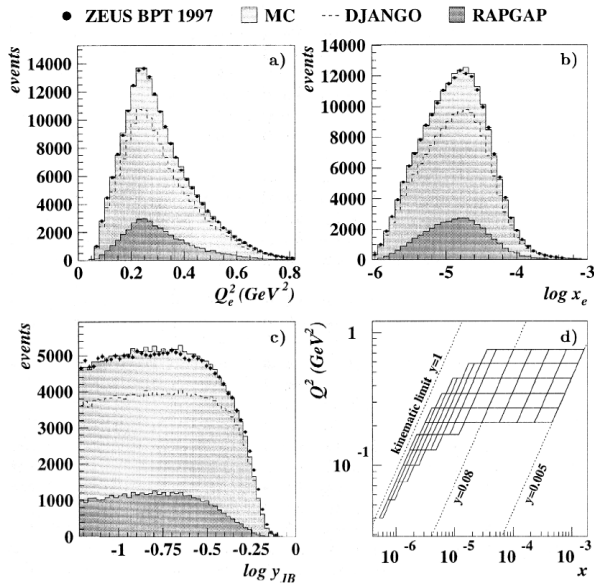
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October 10, 2016

## Low $x$ , low $Q^2$ ZEUS fits to $F_2^p$

- "Measurement of the proton structure function  $F_2$  at very low  $Q^2$  at HERA", J. Breitweg *et al.* (ZEUS Collaboration), Phys.Lett. B487 (2000) 53
- ZEUS 1997 data
- $0.045 \text{ GeV}^2 < Q^2 < 0.65 \text{ GeV}^2$
- $6 \cdot 10^{-7} < x < 1 \cdot 10^{-3}$
- rise of  $F_2$  at low  $x$  slower than observed in HERA data at higher  $Q^2$
- data can be described by Regge theory with a constant logarithmic slope  $\partial \ln F_2 / \partial \ln(1/x)$
- dependence of  $F_2$  on  $Q^2$  stronger than at higher  $Q^2$  values, approaching, at the lowest  $Q^2$  values of this measurement, a region where  $F_2$  becomes nearly proportional to  $Q^2$

# ZEUS low $x$ , low $Q^2$ kinematics



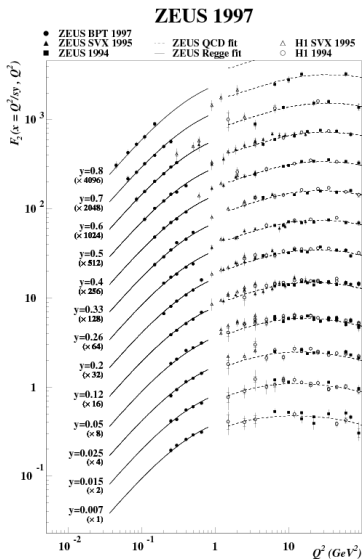
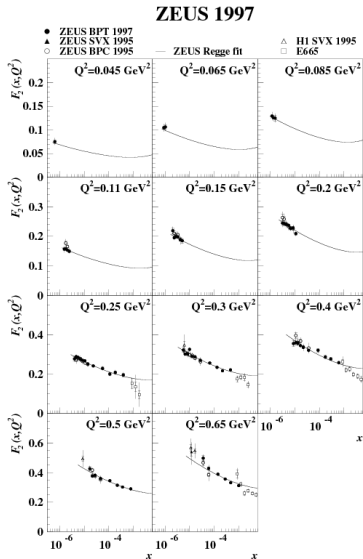
# Phenomenological parameterization

- Based on the combination of a simplified version of the generalized vector meson dominance model for the description of the  $Q^2$  dependence and Regge theory for the description of the  $x$  dependence of  $F_2$ .

$$\text{Fit 1: } F_2(x, Q^2) = \left( \frac{Q^2}{4\pi^2\alpha} \right) \cdot \left( \frac{M_0^2}{M_0^2 + Q^2} \right) \cdot \left( A_{\mathbb{R}} \cdot \left( \frac{Q^2}{x} \right)^{\alpha_{\mathbb{R}} - 1} + A_{\mathbb{P}} \cdot \left( \frac{Q^2}{x} \right)^{\alpha_{\mathbb{P}} - 1} \right)$$

- assuming  $R = 0.165 \cdot Q^2/m_\rho^2$ , w/  $m_\rho = 0.77 \text{ GeV} \Rightarrow F_L = 0$ .
- $A_{\mathbb{R}} = 147.8 \pm 4.6 \mu\text{b}$
- $\alpha_{\mathbb{R}} = 0.5$
- $A_{\mathbb{P}} = 62.0 \pm 2.3 \mu\text{b}$
- $\alpha_{\mathbb{P}} = 1.102 \pm 0.007$
- $M_0^2 = 0.52 \pm 0.04 \text{ GeV}^2$

# $F_2$ and fits



- “ZEUS results on the measurement and phenomenology of  $F_2$  at low  $x$  and low  $Q^2$ ”, J. Breitweg *et al.* (ZEUS Collaboration), Eur.J.Phys. C7 (1999) 609
- New data presented for the first time:  $0.6 < Q^2 < 17 \text{ GeV}^2$ ,  $1.2 \times 10^{-5} < x < 1.9 \times 10^{-3}$  (ZEUS 1995)
- **“The data at very low  $Q^2 < 0.65 \text{ GeV}^2$  are described successfully by a combination of generalised vector meson dominance and Regge theory.”**

## Other fits (2)

$$\text{Fit 2: } \sigma_{\text{tot}}^{\gamma P}(W^2) = A_{\mathbb{R}}(W^2)^{\alpha_{\mathbb{R}}-1} + A_{\mathbb{P}}(W^2)^{\alpha_{\mathbb{P}}-1}$$

- $\alpha_{\mathbb{R}}$  fixed to 0.5 (as the original DL model and other previous estimates)
- $\alpha_{\mathbb{P}} = 1.141 \pm 0.020(\text{stat}) \pm 0.044(\text{syst})$
- $\alpha_{\mathbb{P}} = 1.101 \pm 0.002(\text{stat}) \pm 0.012(\text{syst})$ , fitting both terms to the real photoproduction data (with  $W^2 > 3 \text{ GeV}^2$ ) and BPC  $\sigma_0^{\alpha P}$  data
- $\alpha_{\mathbb{P}} = 1.100 \pm 0.002(\text{stat}) \pm 0.012(\text{syst})$ , including in addition two direct measurements from HERA
- At HERA energies the Reggeon contribution is negligible
- The results are compatible with the DL value of 1.08 and the then best estimate of  $1.0964^{+0.0115}_{-0.0094}$  (Cudell et al., hep-ph/9701312)

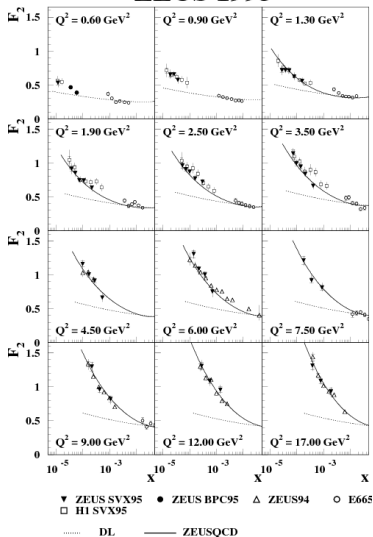
## Other fits (3)

$$\text{Fit 3: } \sigma_{\text{tot}}^{\gamma^p}(W^2, Q^2) = \left( \frac{M_0^2}{M_0^2 + Q^2} \right) [A_{\mathbb{R}}(W^2)^{\alpha_{\mathbb{R}}-1} + A_{\mathbb{P}}(W^2)^{\alpha_{\mathbb{P}}-1}]$$

- $M_0^2$  fixed to 0.53 found before
- $\alpha_{\mathbb{R}}$  fixed at 0.5
- Parameters found by fitting the photoproduction data (with  $W^2 > 3 \text{ GeV}^2$ , but without the two original HERA measurements) and the measured BPC data:
  - ▶  $A_{\mathbb{R}} = 145 \pm 0.2 \mu\text{b}$
  - ▶  $A_{\mathbb{P}} = 63.5 \pm 0.9 \mu\text{b}$
  - ▶  $\alpha_{\mathbb{P}} = 1.097 \pm 0.002$
  - ▶  $\chi^2/ndf = 1.12$
- Parameters do not change (within errors with the two HERA measurements)



## ZEUS 1995

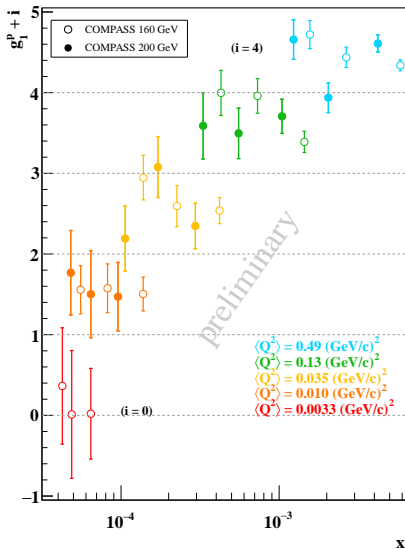


# Current status

- N.B.: the  $\chi^2$  scan to a combined fit of type  $g_1^P(Q^2, x) = x^{-\alpha_R} \cdot \beta$  had yielded  $\alpha_R = 0.31 \pm 0.14$  [[https://compassvm03.cern.ch/elog/Low\\_x.Low\\_Q2/39](https://compassvm03.cern.ch/elog/Low_x.Low_Q2/39)]
- Started to fit models of the same type of ZEUS to the  $g_1^P(x, \nu)$  from COMPASS
- Fit of type 2:  $g_1^P(W^2) = A_R(W^2)^{\alpha_R} + A_P(W^2)^{\alpha_P}$ 
  - ▶  $\alpha_R$  fixed at 0.5
  - ▶  $A_R = -12.358 \pm 0.044$
  - ▶  $A_P = 0.9978 \pm 0.0032$
  - ▶  $\alpha_P = 1.03483 \pm 0.00016$
  - ▶  $\chi^2/ndf = 174/(210 - 24 * 3) \simeq 1.26$  (Prob=2.0%)
- Fit of type 3:  $g_1^P(W^2, Q^2) = \left( \frac{M_0^2}{M_0^2 + Q^2} \right) [A_R(W^2)^{\alpha_R} + A_P(W^2)^{\alpha_P}]$ 
  - ▶  $\alpha_R$  fixed at 0.5
  - ▶  $A_R = -11.3 \pm 0.1$
  - ▶  $A_P = 1.421 \pm 0.013$
  - ▶  $\alpha_P = 1.0020 \pm 0.0006$
  - ▶  $\chi^2/ndf = 183/(210 - 24 * 3) \simeq 1.32$  (Prob=0.65%)
- Work ongoing

# BACKUP

# $g_1^P$ in bins of $Q^2$ and $x$



# Regge fits to $g_1^p(Q^2, x)$

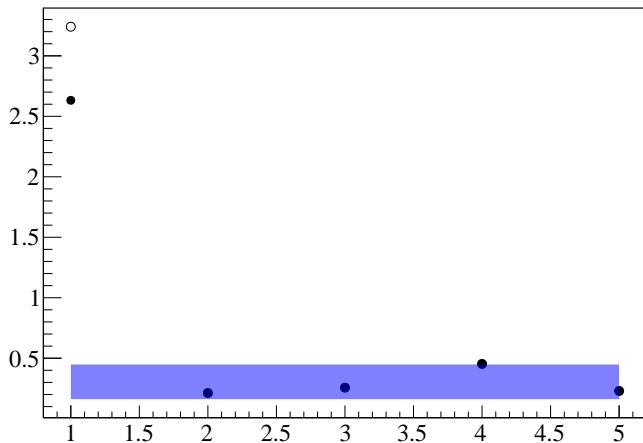
fit function:  $g_1^p(Q^2, x) = x^\alpha \cdot \beta(Q^2)$

$Q^2$ bin	$\chi^2$ (ndf=4)	$\alpha$	$\delta\alpha$	$\beta$	$\delta\beta$
1	2.04721	$-2.63223 \cdot 10^{+0}$	$1.50840 \cdot 10^{+0}$	$1.07052 \cdot 10^{-12}$	$1.83932 \cdot 10^{-11}$
2	0.153038	$-2.11852 \cdot 10^{-1}$	$6.04754 \cdot 10^{-1}$	$7.49732 \cdot 10^{-2}$	$4.25486 \cdot 10^{-1}$
3	4.59496	$-2.56519 \cdot 10^{-1}$	$3.26944 \cdot 10^{-1}$	$7.15864 \cdot 10^{-2}$	$1.96088 \cdot 10^{-1}$
4	4.63522	$-4.52824 \cdot 10^{-1}$	$2.46074 \cdot 10^{-1}$	$2.56648 \cdot 10^{-2}$	$4.58531 \cdot 10^{-2}$
5	14.1419	$-2.29338 \cdot 10^{-1}$	$2.08887 \cdot 10^{-1}$	$1.17238 \cdot 10^{-1}$	$1.39249 \cdot 10^{-1}$

fit function:  $g_1^p(Q^2, x) = x^{-\alpha} \cdot \beta(Q^2)$

$Q^2$ bin	$\chi^2$ (ndf=4)	$\alpha$	$\delta\alpha$	$\beta$	$\delta\beta$
1	2.03244	$3.24061 \cdot 10^{+0}$	$1.10475 \cdot 10^{+0}$	$2.49855 \cdot 10^{-15}$	$3.00028 \cdot 10^{-14}$
2	0.153039	$2.12433 \cdot 10^{-1}$	$7.80963 \cdot 10^{-1}$	$7.45638 \cdot 10^{-2}$	$5.46468 \cdot 10^{-1}$
3	4.59496	$2.56530 \cdot 10^{-1}$	$3.90718 \cdot 10^{-1}$	$7.15798 \cdot 10^{-2}$	$2.34315 \cdot 10^{-1}$
4	4.63522	$4.52837 \cdot 10^{-1}$	$2.64183 \cdot 10^{-1}$	$2.56623 \cdot 10^{-2}$	$4.89501 \cdot 10^{-2}$
5	14.1419	$2.29363 \cdot 10^{-1}$	$2.25731 \cdot 10^{-1}$	$1.17223 \cdot 10^{-1}$	$1.50459 \cdot 10^{-1}$

# Values of $\alpha$ per bin



$\chi^2$  scan to a combined fit of type  $g_1^p(Q^2, x) = x^{-\alpha_0} \cdot \beta$

